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| Simpson Aerospace: Solution to Homework 1 |

Objective: Explain how the Newton-Raphson method is used for vectors

**TO:** Statistical Orbit Determination Class

**CC:**

**REF:**

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**Memo:** SimpsonAerospace: Lectures

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**SUMMARY:**

Problem 1 provides the solution for us. We are learning how to use iterative methods to estimate the state vector. In this case we will use the Newton-Raphson root-finding method to solve for the problem. An Excel sheet is provided that walks through the first three iterations as an illustration. C++ code is provided on GitHub that will solve for the final solution and show the number of iterations.

**OVERVIEW:**

Given a set of unitless initial conditions, we are told that only the range observations and the ground station position are accurate. We will solve iteratively using the Newton iteration scheme covered previously.

We are given the final answer to confirm our iterative solution.

*Solution*

The pseudo-range, , for the uniform gravitational field is determined by . and are both dependent on . is also dependent upon in this two-dimensional field. This is important because in order to use the Newton iteration method, we need to find . We do this by taking a first-order Taylor series expansion and neglecting higher terms.

The term, is the next iteration of the iteration scheme. Subtracting the next iteration from the current provides us with the residuals or . Multiplying these by the inverse of the mapping matrix gives us the residuals of the state vector.

Having found the residuals of our state vector we can now add this to our original state vector to determine the next iteration of the state vector. The Excel spreadsheet shows this process very clearly without calculating the relative error for each step.